## Goldsmith

Primary Academy
A part of the Windsor Academy Trust

# Number and Calculation Policy 

Reviewed: January 2024

Next Review: January 2025

## Contents:

> Goldsmith Primary Academy - Maths Approach on a Page - 3 ARK Maths Mastery - Progression in Calculations Document - 6 ARK Maths Mastery - Progression in Vocabulary Document - 79

## Intent:

At Goldsmith we develop competent mathematicians who are equipped with the appropriate knowledge and skills to succeed in the modern world. This curriculum covers all content of the National Curriculum (2014). Through this curriculum, we develop fluent mathematicians who challenge themselves by reasoning and problem solving, as a matter of course, in each lesson. We endeavour to model mathematical structures, using concrete apparatus, enabling pupils to represent their mathematical knowledge in pictorial or abstract form.

## Implementation:

## - What is our curriculum:

In our school, we have implemented the ARK Mastery Maths Programme of Study for primary pupils. This is a highly practical and visual approach to a mastery curriculum and enables pupils to visualise problems in addition to solving them. Details of the subject matter being taught can be found in the ARK Mastery Maths Overview document. Additionally, details of how we teach calculations can be found in the ARK Mastery Maths Progression in Calculations document. We can divide our curriculum into five sub-curricula:
-ARK Mastery Maths Content Teaching
-ARK Mastery Maths Meetings
-ARK Same Day Catch-Up
-Multiplication Tables
-Arithmetic

## ARK Mastery Maths Content:

EYFS - As per Development Matters, pupils in Nursery and Goldilocks are encouraged to investigate numbers and quantities in engaging, hands-on activities. Pupils are encouraged to make links between numbers and associated quantities of objects or manipulatives. In Reception, pupils are moved on to the ARK curriculum for EYFS Maths, receiving two maths lessons per week which are adult led, resulting in either an adult led activity to consolidate new knowledge or independent opportunities in Enhanced Provision. Children are also able to engage in maths-led activities throughout the week, which are based on the topic being covered. On Friday, teachers in Reception engage in personalised learning, ensuring that any gaps in knowledge are addressed quickly.

KS1 and KS2 - In KS1 and 2, pupils undertake four ARK Mastery Maths lessons per week. Teaching is borne of the concrete, pictorial, abstract approach to mathematics teaching and enables pupils to demonstrate their new knowledge in a variety of ways, using manipulatives. Pupils' tasks are differentiated in order to enable ALL to achieve the learning objective. We use a simple Green (Working Towards), Yellow (Working At) and Red (Working Beyond) system, to signify the tasks being completed. Pupils are actively encouraged to move through the colour groups, should they be confident with a concept being taught. All pupils are aware they should be aiming for the yellow task or beyond. Manipulative maths equipment is used in all maths lessons, either by direct instruction of the teacher or available on the maths "Enable Station." Equipment designed for regular use is contained within a 1:2 CPA toolkit box.

## ARK Mastery Maths Meetings:

KS1 and KS2 - Pupils take part in "Maths Meetings" for 15 minutes in the afternoon session (3x/week in KS1 $4 x /$ week in KS2). These sessions are deliberately set apart from the main content teaching as they focus on engaging and activating prior knowledge. In all year groups, pupils are assessed using a grid of questions. Teachers then gap analyse this information and teach the identified gaps in subsequent maths meetings. Pupils then undertake a Maths Meeting assessment every two weeks, which should illustrate that teaching has addressed knowledge gaps. Multiplication table practice will also take place in these sessions.

## ARK Same Day Catch-Up:

KS1 and KS2 - Pupils who do not succeed during teaching sessions will be identified by the class teacher to receive an 'SDCU' intervention. Pupils will work with a teacher or teaching assistant to have a second chance to learn a concept, the same day it has been taught. This takes place $4 x /$ week in KS1 and KS2.

## Multiplication Tables:

EYFS - Pupils have access to a "Numbots" login which teachers may use as an activity during free-flow play or as a direct teaching tool, later in reception. Numbots enables pupils to experience numbers in different context and begin to make simple addition and subtraction sentences, as pupils progress through the "Number Story."

KS1 - Pupils are given individual access to "Times Tables Rock Stars." Pupils are able to access this at home and in school during one maths meeting per week. In school and across our academy trust, we have frequent competitions to ensure engagement.

KS2 - As in KS1, pupils have access to their own TTRS login. Pupils are able to use this in school during one of their timetabled maths meetings. In addition, pupils in KS2 take part in the weekly 99 Club. Children demonstrate progress by completing a given number of questions in a given time. Pupils receive a certificate on successful graduation from a club. KS2 pupils will undertake the 99 Club in maths meeting time.

## Arithmetic:

KS1 and KS2 - Arithmetic is timetabled as the fifth lesson of the week and is used in different ways on a bi-weekly basis. In week 1, pupils will be assessed on their arithmetic knowledge bi-weekly. In the initial session, pupils will undertake the test and then peer and shared mark the assessment, with the teacher modelling answers. In week 2, children will complete their Maths Meeting Assessment (30 mins) and take part in an arithmetic gap filling session based on the gap analysis of the previous week's arithmetic test data.

## Impact:

- How is impact measured?


## ARK Mastery Maths Content, ARK Mastery Maths Meetings and Arithmetic:

Impact of our curriculum is measured in several ways. On a daily basis, pupils' progress is measured through our \#FeedForward policy; pupils are given next steps verbally and in their books. At the beginning and end of the unit, pupils are given pre- and post-unit quizzes. This enables teachers to plan for pupils' needs and identify and address gaps, where necessary. On a termly basis, pupils sit NTS mathematics assessments in arithmetic and reasoning. This data is also gap analysed in order to inform future planning and maths meeting foci. Impact of teaching is also quality assured through learning walks and lesson observation. Finally, the impact of the pupil's whole mathematical journey is measured in end-of-key-stage assessments in the EYFS, KS1 and KS2. This data is published nationally.

## Multiplication Tables:

Impact of our multiplication tables curriculum is measured by progress pupils make; through levels on TTRS, Clubs in the 99 club and more formally, in the Year 4 Multiplication Tables Check.

## - How do we know children have made progress?

There are several means of identifying progress in mathematics. The simplest is to identify the progression of pupils through the coloured groups on offer in our mathematics lessons. As previously mentioned, our pupils know they are aiming for the yellow task - working at year group standard. Pupils standardised scores, derived from performance in NTS assessments, are also key in identifying areas for development. As part of the GADY project (Goldsmith Attainment in Disadvantaged Youngsters), pupils are required to improve their standardised score by a set number of points in each term of assessment. This enables staff to see the important part they are playing in any child's progression through the math curriculum.

- How do we challenge and support lack of progress?

Teachers are challenged and supported through pupil's lack of progress during pupil progress meetings. Teachers are able to highlight any concerns about a child, whilst providing solutions to assist that child in their continued study. SLT and the teacher together, may decide upon offering additional intervention to the pupil. Teachers and SLT will also endeavour to engage home in supporting in school learning, through home learning and IEP home
packs.

## How are we inclusive?

We believe every child should be able to access our maths curriculum. We feel that by offering quality first teaching to all, in addition to targeted and appropriate use of concrete resources, pictorial representations and eventual exposure to abstract calculations, all pupils can succeed.

In all classrooms, CPA toolkits can be found which allows children 1:2 access to the equipment used in many mathematical teaching models (Numicon, Base 10, Place Value Counters, Bead Strings)


Should pupils struggle in mathematics, additional support will always be given by teachers and teaching assistants in order to ensure that pupils achieve. Pupils are targeted for same day intervention, $4 \mathrm{x} /$ week, to be given a second opportunity to grasp a concept. If necessary, pupils will be identified as part of pupil progress meeting procedures and will be given extra intervention.

## Mathematics Mastery

## Progression in calculations

## Year 1 - Year 6*

NB. Users should familiarise themselves with the introduction (pp 2-10) to this document before referring to individual year group guidance.
*Progression guidance is not provided for EYFS/Reception since the focus should be on the understanding of early number concepts and number sense through the use of concrete manipulatives, as exemplified in the programmes of study.

## Introduction

At the centre of the mastery approach to the teaching of mathematics is the belief that all pupils have the potential to succeed. They should have access to the same curriculum content and, rather than being extended with new learning, they should deepen their conceptual understanding by tackling challenging and varied problems. Similarly, with calculation strategies, pupils must not simply rote learn procedures but demonstrate their understanding of these procedures through the use of concrete materials and pictorial representations. This document outlines the different calculation strategies that should be taught and used in Years 1 to 6, in line with the requirements of the 2014 Primary National Curriculum.

## Background

The 2014 Primary National Curriculum for mathematics differs from its predecessor in many ways. Alongside the end of Key Stage year expectations, there are suggested goals for each year; there is also an emphasis on depth before breadth and a greater expectation of what pupils should achieve.

One of the key differences is the level of detail included, indicating what pupils should be learning and when. This is suggested content for each year group, but schools have been given autonomy to introduce content earlier or later, with the expectation that by the end of each key stage the required content has been covered.

For example, in Year 2, it is suggested that pupils should be able to 'add and subtract one-digit and two-digit numbers to 20 , including zero' and a few years later, in Year 5, they should be able to 'add and subtract whole numbers with more than four digits, including using formal written methods (columnar addition and subtraction)'.

In many ways, these specific objectives make it easier for teachers to plan a coherent approach to the development of pupils' calculation skills, and the expectation of using formal methods is rightly coupled with the explicit requirement for pupils to use multiple representations, including concrete manipulatives and images or diagrams - a key component of the mastery approach.

## Purpose

The purpose of this document is threefold. Firstly, in this introduction, it outlines the structures for calculations, which enable teachers to systematically plan problem contexts for calculations to ensure pupils are exposed to both standard and non-standard problems. Secondly, it makes teachers aware of the strategies that pupils are formally taught within each year group, which will support them to perform mental and written calculations. Finally, it supports teachers in identifying appropriate pictorial representations and concrete materials to help develop understanding.

The policy only details the strategies; teachers must plan opportunities for pupils to apply these, for example, when solving problems, or where opportunities emerge elsewhere in the curriculum.

## How to use the document

For each of the four rules of number, different strategies are laid out, together with examples of what concrete materials can be used and how, along with suggested pictorial representations. Please note that the concrete and pictorial representation examples are not exhaustive, and teachers and pupils may well come up with alternatives. The purpose of using multiple representations is to give pupils a deep understanding of a mathematical concept and they should be able to work with and explain concrete, pictorial and abstract representations, and explain the links between different representations. Depth of understanding is achieved by moving between these representations. For example, if a child has started to use a pictorial representation, it does not mean that the concrete
cannot be used alongside the pictorial. If a child is working in the abstract, depth can be evidenced by asking them to exemplify their abstract working using a concrete or pictorial representation and to explain what they have done using the correct mathematical vocabulary; language is, of course, one abstract representation but is given particular significance in the national curriculum.

## Mathematical language

The 2014 National Curriculum is explicit in articulating the importance of pupils using the correct mathematical language as a central part of their learning. Indeed, in certain year groups, the non-statutory guidance highlights the requirement for pupils to extend their language around certain
"The quality and variety of language that pupils hear and speak are key factors in developing their mathematical vocabulary and presenting a mathematical justification, argument or proof."

2014 Maths Programme of Study concepts.

Suggested language structures accompany each strategy outlined in this document. These build on one another systematically, which supports pupils in making links between and across strategies as they progress through primary school.

| $\checkmark$ | $\mathbf{x}$ |
| :--- | :--- |
| ones | units |
| is equal to | equals / makes |
| zero | oh (the letter O) | New vocabulary should be introduced in a suitable context (for example, with relevant real objects, manipulatives, pictures or diagrams) and explained precisely. High expectations of the mathematical language used are essential, with teachers modelling accurate mathematical vocabulary and expecting pupils' responses to include it infull sentences.

## Presentation of calculations

You will see that throughout this document, calculations are presented in a variety of ways. It is important for pupils' mathematical understanding to experience and work with calculations and missing numbers in different positions relative to the $=$ symbol. Examples used in classwork and independent work should reflect this.

## Estimation

Pupils are expected to use their developing number sense from Year 1 to make predictions about the answers to their calculations. As their range of mental strategies increases, these predictions and, later, estimates should become increasingly sophisticated and accurate. All teaching of calculation should emphasise the importance of making and using these estimates to check, first, the sense and, later, the accuracy of their calculations.

## Developing number sense

Fluency in arithmetic is underpinned by a good sense of number and an ability to understand numbers as both a concept (e.g. 7 is the value assigned to a set of seven objects) and as something resulting from a process (three beads and four more beads gives seven beads altogether or $3+4=7$ ). Understanding that a number can be partitioned in many ways (e.g. $7=4+3 ; 5+2=7 ; 1+6=7$ ) is key to being able to use numbers flexibly in calculating strategies. The part-whole model and, later, bar models, are particularly useful for developing a relational understanding of number. Pupils who are fluent in number bonds (initially within ten and then within twenty) will be able to use the 'Make ten' strategy efficiently, enabling them to move away from laborious and unreliable counting strategies, such as 'counting all' and 'counting on'. Increasing fluency in efficient strategies will allow pupils to develop flexible and interlinked approaches to addition and subtraction. At a later stage, applying multiplication and division facts, rather than relying on skip-counting, will continue to develop flexibility with number.

## Structures and contexts for calculations

There are multiple contexts (the word problem or real-life situation, within which a calculation is required) for each mathematical operation (i.e. addition) and, as well as becoming fluent with efficient calculating strategies, pupils also need to become fluent in identifying which operations are required. If they are not regularly exposed to a range of different contexts, pupils will find it difficult to apply their understanding of the four operations. For each operation, a range of contexts can be identified as belonging to one of the conceptual 'structures' defined below.

The structure is distinct from both the operation required in a given problem and the strategy that may be used to solve the calculation. In order to develop good number sense and flexibility when calculating, children need to understand that many strategies (preferably the most efficient one for them!) can be used to solve a calculation, once the correct operation has been identified. There is often an implied link between the given structure of a problem context and a specific calculating strategy. Consider the following question: A chocolate bar company is giving out free samples of their chocolate on the street. They began the day with 256 bars and have given away 197. How many do they have remaining? The reduction context implicitly suggests the action of 'taking away' and might lead to a pupil, for example, counting back or using a formal algorithm to subtract 197 from 256 (seeing the question as $256-197=\square$ ). However, it is much easier to find the difference between 197 and 256 by adding on (seeing the question as $197+\square=256$ ). Pupils with well-developed number sense and a clear understanding of the inverse relationship between addition and subtraction will be confident in manipulating numbers in this way.

Every effort is made to include multiple contexts for calculation in the Mathematics Mastery materials but, when teachers adapt the materials (which is absolutely encouraged), having an awareness of the different structures and being sure to include a range of appropriate contexts, will ensure that pupils continue to develop their understanding of each operation. The following list should not be considered to be exhaustive but defines the structures (and some suggested contexts) that are specifically included in the statutory objectives and the non-statutory guidance of the national curriculum. Specific structures and contexts are introduced in the Mathematics Mastery materials at the appropriate time, according to this guidance.

## Importance of knowns vs unknowns and using part-whole understanding

One of the key strategies that pupils should use to identify the correct operation(s) to solve a given problem (in day-to-day life and in word problems) is to clarify the known and unknown quantities and identify the relationships between them. Owing to the inverse relationship between addition and subtraction, it is better to consider them together as 'additive reasoning', since changing which information is unknown can lead to either addition or subtraction being more suitable to calculate a solution for the same context. For the same reason, multiplication and division are referred to as 'multiplicative reasoning'. Traditionally, approaches involving key vocabulary have been the main strategy used to identify suitable operations but owing to the shared underlying structures, key words alone can be ambiguous and lead to misinterpretation (see for example the question below about Samir and Lena, where the key word 'less' might be identified, but addition is required to solve the problem).

A more effective strategy is to encourage pupils to establish what they know about the relationship between the known and unknown values and if they represent a part or the whole in the problem, supported through the use of part-whole models and/or bar models. In the structures exemplified

## Mathematics Mastery

below, the knowns and unknowns have been highlighted. Where appropriate, the part-whole relationships have also been identified. Pupils should always be given opportunities to identify and discuss these, both when calculating and when problem-solving.

## Standard and non-standard contexts

Using key vocabulary as a means of interpreting problems is only useful in what are in this document defined as 'standard' contexts, i.e. those where the language is aligned with the operation used to solve the problem. Take the following example:

First there were 12 people on the bus. Then three more people got on. How many people are on the bus now?

Pupils would typically identify the word 'more' and assume from this that they need to add the values together, which in this case would be the correct action. However, in non-standard contexts, identifying key vocabulary is unhelpful in identifying a suitable operation. Consider this question:

First there were 12 people on the bus and then some more people got on at the school. Now there are 15 people on the bus. How many people got on at the school?

Again the word 'more' would be identified, and a pupil may then erroneously add together 12 and 15 . It is therefore much more helpful to consider known and unknown values and the relations between them.

Overexposure to standard contexts and lack of exposure to non-standard contexts will mean pupils are more likely to rely on 'key vocabulary' strategies, as they see that this works in most of the cases they encounter. It is therefore important, when adapting lesson materials, that non-standards contexts are used systematically, alongside standard contexts.

Additive reasoning

## Change structures

## augmentation (increasing)

where an existing value has been added to

## Standard

First there were 12 people on the bus. Then three more people got on. How many people are on the bus now?

"I know both parts. My first part is twelve and my second part is three. I don't know the whole. I need to add the parts of twelve and three to find the whole."

$$
12+3=\text { ? }
$$

## Non-standard

First there were 12 people on the bus and then some more people got on at the school. Now there are 15 people on the bus. How many people got on at the school?

"I know my first part is twelve and I know the whole is 15. I don't know the value of the second part. To find the second part, I could add on from 12 to make 15 or I could subtract 12 from 15."

$$
12+?=15 \quad 15-12=?
$$

## Non-standard

First there were some people on the bus then it stopped to pick up three more passengers at the bank.
Altogether now there are 15 people on the bus. How many were people were on the bus before it stopped at the bank?
"I know the value of the second part is three and that the whole is 15 . I don't know the value of the first part. To find the first part, I could add on from three to make 15 or I could subtract three from 15."

$$
?+3=15 \quad 15-3=?
$$

## reduction (decreasing)

where an existing value has been reduced

## Standard

First Kieran had six plates in his cupboard. Then he took two plates out to use for dinner. How many plates are in the cupboard now?
 "I know the whole is six. I know one of the part that has been taken away is two. I don't know the other part. I need to subtract the known part, two, from the whole, six, to find the remaining part."

$$
6-2=? \quad 2+?=6
$$

## Non-standard

First there were six plates in the cupboard. Then Kieran took some out for dinner. There are now four plates left in the cupboard. How
 many did Kieran take out?
"I know the whole is six and the remaining part is four. I don't know the part that was taken away. To find the part that was taken away I can add on from four to make six or I could subtract four from six."

$$
6-?=4 \quad 6-4=?
$$

## Non-standard

First there were some plates in the cupboard. Then Kieran took two out for dinner. Now there are four left. How many plates were in the cupboard to start with?

"I know the part that has been taken away is two and the part that is left is four. I don't know the whole. I can find the whole by adding the parts of four and two."

$$
?-2=4 \quad 2+4=?
$$

Note: the 'first... then... now' structure is used heavily in KS1 to scaffold pupils' understanding of change structures. Once pupils are confident with the structures, such linguistic scaffolding can be removed, and question construction can be changed to expose pupils to a greater range of nuance in interpreting problems. For example, the second and third reduction problems could be reworded as follows:

Kieran took two plates out of his cupboard for dinner. There were four left. How many plates were in the cupboard to begin with?

There were six plates in the cupboard before Kieran took some out for dinner. If there were four plates left in the cupboard, how many did Kieran take out?

These present the same knowns and unknowns, and therefore the same bar models and resulting equations to solve the problems; however, the change in wording makes them more challenging to pupils who have only worked with a 'first... then... now' structure so far.

## Part-whole structures

## Combination (aggregation)/partitioning

combining two or more discrete quantities/splitting one quantity into two or more sub-quantities
Hakan and Sally have made a stack of their favourite books. Four books belong to Hakan, three to Sally. How many books are in the stack altogether?
"I know both parts. One part is four and the other part is three. I don't know the whole.
I need to add the parts of three and four to find the whole."

$$
4+3=? \quad 3+4=?
$$


(Only one problem has been written for combination as, owing to the commutativity of addition, the only change in question wording would be to swap Hakan and Sally's names. The resulting bar model and calculation would be identical.)

Sally and Hakan have made a stack of their favourite books. There are seven books altogether. If three of them are Sally's, how many belong to Hakan?
"I know the whole is seven and that one of the parts is three. I don't know the other part. I need to add on from three to make seven or subtract three from seven to find the other part."


$$
3+?=7 \quad 7-3=?
$$

Sally and Hakan have made a stack of their favourite books. There are seven books altogether. If four of them are Hakan's, how many belong to Sally?
"I know the whole is seven and that one of the parts is four. I don't know the other part. I need to add on from four to make seven or subtract four from seven to find the other part."


$$
4+?=7 \quad 7-4=?
$$

Note: all part-whole contexts are considered to be 'standard', as the language of part-whole is unambiguous.

## Comparison structures

Comparison structures involve a relationship between two quantities; their relationship is expressed as a difference. The structures vary by which of the values are known/unknown (the larger quantity, the smaller quantity and/or their difference). Part-whole language is not used here because the context contains not one single 'whole', but instead two separate quantities and it is the relationship between them being considered. Comparison bar models are therefore used to model these structures, which are known to be the most challenging for pupils to interpret.

## Smaller quantity and larger quantity are known (comparative difference)

## Standard

Navin has saved $£ 19$ from his pocket money. Sara has saved $£ 31$ from her pocket money. How much more has Sara saved than Navin? or How much less has Navin saved than Sara?
"I know one quantity is 19 and the other quantity is 31 . I don't know the difference. To find the difference I could add on from 19 to make 31 or I could subtract 19 from 31."


$$
19+?=31 \quad 31-19=?
$$

## Smaller quantity and difference are known (comparative addition)

## Standard

Ella has six marbles. Robin has three more than Ella. How many marbles does Robin have?
"I know the smaller quantity is six. I know the difference is three. I don't know the larger quantity. To find the larger quantity I need to add three to six."


$$
6+3=?
$$

## Non-standard

Samir and Lena are baking shortbread but Lena's recipe uses 15 g less butter than Samir's. If Lena needs to use 25 g of butter, how much does Samir need?
"I know the smaller quantity is 25 . I know the difference between the quantities is 15 . I don't know the larger quantity. To find the larger quantity I need to add 15 to 25 ."


$$
?-15=25 \quad 25+15=\text { ? }
$$

## Larger quantity and difference are known (comparative subtraction)

## Non-standard

Ella has some marbles. Robin has three more than Ella and he has nine marbles in total. How many marbles does Ella have?
"I know the larger quantity is nine. I know the difference between the quantities is three. I don't know the smaller quantity. To find the smaller quantity I need to add on from three to make nine or subtract three from nine."

$$
?+3=9 \quad 9-3=?
$$



## Standard

Samir's shortbread recipe uses 40 g of butter. Lena's recipe uses 15 g less butter. How much butter does Lena need?
"I know one quantity is 40 . I know the difference between the quantities is 15 . I don't know the smaller quantity but I know it is 15 less than 40 . To find the smaller quantity, I need to subtract 15 from 40."


$$
40-15=? \quad ?+15=40
$$

## Multiplicative reasoning

| Repeated grouping structures |  |
| :---: | :---: |
| repeated addition <br> groups (sets) of equal value are combined or repeatedly added <br> There are four packs of pencils. Each contains five pencils. How many pencils are there? <br> "I know there are four equal parts and that each part has a value of five. I don't know the value of the whole. To find the whole, I need to multiply four and five." $\begin{array}{r} 5+5+5+5=? \\ 5 \times 4=? \end{array}$ | repeated subtraction (grouping) <br> groups (sets) of equal value are partitioned from the whole or repeatedly subtracted <br> There are 12 counters. If each child needs three counters to play the game, how many children can play? <br> "I know the whole is twelve and that the value of each equal part is three. To find the number of equal parts, I need to know how many threes are in twelve." $3 \times ?=12 \quad 12 \div 3=?$ <br> sharing (into equal groups) <br> the whole is shared into a known number (must be a positive integer) of equal groups (sets) <br> Share twelve counters equally between three children. How many counters does each child get? <br> "I know the whole is twelve and the number of equal parts is three. I don't know the value of each part. To find the value of each part, I need to know what goes into twelve three times." $? \times 3=12 \quad 12 \div 3=?$ |
| Cartesian product of two measures |  |
| correspondence <br> calculating the number of unique combinations that can be created from two (or more) sets <br> Robin has three different hats and four different tops. How many different outfits can he create, that combine one hat and one top? <br> "I know how many hats there are and I know how many tops there are. I don't know the number of different outfits that can be created. To find the number of outfits, I need to find how many different tops can be worn with each hat or how many different hats can be worn with each top." $4 \times 3=\text { ? }$ <br> $3 \times 4=$ ? |  |



## Progression in calculations Year 1

## National curriculum objectives linked to addition and subtraction

## These objectives are explicitly covered through the strategies outlined in this document:

- Add and subtract one-digit and two-digit numbers to 100, including zero (N.B. Year 1 N.C. objective is to do this with numbers to 20 ).
- Add and subtract numbers using concrete objects, pictorial representations, and mentally, including: a two-digit number and ones, a two-digit number and tens, 2 two-digit numbers; add 3 one-digit numbers (Year 2).
- Represent and use number bonds and related subtraction facts within 20.
- Given a number, identify 1 more and 1 less.
- Show that addition of two numbers can be done in any order (commutative) but subtraction of one number from another cannot (Year 2).
- Recognise the inverse relationship between addition and subtraction and use this to solve missing number problems (Year 2).

The following objectives should be planned for lessons where new strategies are being introduced and developed:

- Read, write and interpret mathematical statements involving addition (+), subtraction (-) and equal (=) signs.
- Solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems, such as $7=\square-9$.
- Solve problems with addition and subtraction:
- Using concrete objects and pictorial representations, including those involving numbers, quantities and measures
- Applying their increasing knowledge of mental methods

Teachers should refer to the definitions and guidance on the structures for addition and
subtraction to provide a range of appropriate real-life contexts for calculations.

Y1 Addition


Adding 1, $\mathbf{2}$, $\mathbf{3}$ more
Here the emphasis
should be on the
language rather than
the strategy. As pupils
are using the
beadstring, ensure that
they are explaining
using language such
ss;
' more than 5 is equal
to 6.'
'2 more than 5 is equal
to 7. .
'8 is 3 more than 5.'
Over time, pupils
should be
encouraged to rely
more on their
number bonds
knowledge than on
counting strategies.

## Partitioning to add (no regrouping)

Place value grids and Dienes blocks could be used as shown in the diagram before moving onto pictorial representations. Dienes blocks should always be available, as the main focus in Year 1 is the concept of place value rather than mastering the procedure.

When not regrouping, partitioning is a mental strategy and does not need formal recording in columns. This representation prepares them for using column addition with formal recording.

## Introducing column

 method for addition, regrouping onlyDienes blocks and place value grids should be used as shown in the diagrams. Even when working pictorially, pupils should have access to Dienes blocks.

See additional guidance on unit pages
 for extra guidance on this strategy.


## Y1 Subtraction

| Strategy \& guidance | CPA |
| :---: | :---: |
| Taking away from the ones <br> When this is first introduced, the concrete representation should be based upon the diagram. Real objects should be placed on top of the images as one-to-one correspondence so that pupils can take them away, progressing to representing the group of ten with a tens rod and ones with ones cubes. |  |
| Counting back Subtracting 1, 2, or 3 by counting back <br> Pupils should be encouraged to rely on number bonds knowledge as time goes on, rather than using counting back as their main strategy. | $16-2=14$ |

Mathematics
Mastery


| Taking away from |
| :--- | :--- |
| the tens |
| Pupils should identify |
| that they can also take |
| away from the tens |
| and get the same |
| answer. |
| This reinforces their |
| knowledge of number |
| bonds to 1o and |
| develops their |
| application of number |
| bonds for mental |
| strategies. |

Mathematics Mastery

| Subtracting multiples of ten Using the vocabulary of 1 ten, 2 tens, 3 tens etc. alongside 10, 20 , 30 is important as pupils need to understand that it is a ten not a one that is being taken away. | $40=60-20$ |  |
| :---: | :---: | :---: |
| Column method with regrouping <br> This example shows how pupils should work practically when being introduced to this method. <br> There is no formal recording in columns in Year 1 but this practical work will prepare pupils for formal methods in Year 2. <br> See additional guidance on unit pages to support with this method. |  |  |

## National Curriculum objectives linked to multiplication and division

These objectives are explicitly covered through the strategies outlined in this document:

- Solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.

Teachers should refer to definitions and guidance on the structures for multiplication and division to provide a range of appropriate real-life contexts for calculations.

Y1 Multiplication

| Strategy \& guidance | CPA |
| :---: | :---: |
| Skip counting in multiples of 2,5 , 10 from zero <br> The representation for the amount of groups supports pupils' understanding of the written equation. So two groups of 2 are 2, 4. Or five groups of 2 are 2, 4, 6, 8, 10 . <br> Count the groups as pupils are skip counting. <br> Number lines can be used in the same way as the bead string. <br> Pupils can use their fingers as they are skip counting. | $4 \times 5=20$ |
| Making equal groups and counting the total <br> How this would be represented as an equation will vary. This could be $2 \times 4$ or $4 \times 2$. The importance should be placed on the vocabulary used alongside the equation. So this picture could represent 2 groups of 4 or 4 twice. | Draw <br> to show $2 \times 3=6$ |


| Solve multiplications <br> using repeated addition | $3 \times 3=3+3+3$ |
| :--- | :--- |
| This strategy helps pupils |  |
| make a clear link between |  |
| multiplication and division |  |
| as well as exemplifying the |  |
| 'repeated addition'structure |  |
| for multiplication. It is a |  |
| natural progression from |  |
| the previous 'count all' |  |
| strategy as pupils can be |  |
| encouraged to 'count on'. |  |
| However, as number bonds |  |
| knowledge grows, pupils |  |
| should rely more on these |  |
| important facts to calculate |  |
| efficiently. |  |

Y1 Division

| Strategy \& guidance | CPA |
| :---: | :---: |
| Sharing objects into groups | $10 \div 2=5$ |
| Pupils should become familiar with division equations through working practically. <br> The division symbol is not formally taught at this stage. | There are 10 sweets. Ring groups of 2. <br>  <br> There are $\qquad$ groups of 2 . |

# Progression in calculations Year 2 

## National Curriculum objectives linked to addition and subtraction

## These objectives are explicitly covered through the strategies outlined in this document:

- Add and subtract numbers using concrete objects, pictorial representations, and mentally, including: a two-digit number and ones; a two-digit number and tens; 2 two-digit numbers; adding three one-digit numbers.
- Add and subtract numbers mentally, including: a three-digit number and ones; a three-digit number and tens; a three-digit number and hundreds (Year 3).
- Recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100 .
- Find 10 or 100 more or less than a given number (Year 3 ).
- Show that addition of two numbers can be done in any order (commutative) but subtraction of one number from another cannot.
- Recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.
- Add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction (Year 3).

The following objectives should be planned for lessons where new strategies are being introduced and developed:

- Solve problems with addition and subtraction: using concrete objects and pictorial representations, including those involving numbers, quantities and measures; apply increasing knowledge of mental and written methods.
- Solve problems, including missing number problems, using number facts, place value and more complex addition and subtraction. (Year 3)

Teachers should refer to the definitions and guidance on the structures for addition and subtraction to provide a range of appropriate real-life contexts for calculations.

## Y2 Addition

| Strategy \& guidance | CPA |
| :---: | :---: |
| Part-part-whole <br> Pupils explore the different ways of making 20. They can do this with all numbers using the same representations. <br> This model develops knowledge of the inverse relationship between addition and subtraction and is used to find the answer to missing number problems. | $\begin{aligned} & 20=17+3 \\ & 20=3+17 \\ & 20-3=17 \\ & 20-17=3 \end{aligned}$ $\begin{gathered} \square+\square=20 \\ \square+\square=\square \\ \square+\square=20 \\ \square+\square \end{gathered}$ $\square$ $+1=16$ <br> $16-1=$ $\square$ <br> $1+$ $\square$ $=16$ <br> 16 - $\square$ |
| Counting on in tens and hundreds |  |

Mathematics Mastery

| Strategy \& guidance | CPA |
| :---: | :---: |
| Using known facts to create derived facts <br> Dienes blocks should be used alongside pictorial and abstract representations when introducing this strategy. |  |
| Partitioning one number, then adding tens and ones <br> Pupils can choose themselves which of the numbers they wish to partition. Pupils will begin to see when this method is more efficient than adding tens and taking away the extra ones, as shown. |  |
| Round and adjust (sometimes known as a compensating strategy) <br> Pupils will develop a sense of efficiency with this method, beginning to see when rounding and adjusting is more efficient than adding tens and then ones. |  $22+17=39$ |

Mathematics Mastery

| Strategy \& guidance | CPA |
| :---: | :---: |
| Make ten strategy <br> How pupils choose to apply this strategy is up to them; however, the focus should always be on efficiency. <br> It relies on an understanding that numbers can be partitioned in different ways in order to easily make a multiple of ten. | $\begin{array}{r} 38+15= \\ 1 \\ 2 \\ 10 \end{array}$ |
| Partitioning to add without regrouping <br> As in Year 1, this is a mental strategy rather than a formal written method. Pupils use the Dienes blocks (and later, images) to represent 3digit numbers but do not record a formal written method if there is no regrouping. |  |
| Column method with regrouping <br> Dienes blocks should be used alongside the pictorial representations; they can be placed on the place value grid before pupils make pictorial representations. <br> As in Year 1, the focus for the column method is to develop a strong understanding of place value. |  |

## Y2 Subtraction

| Strategy \& guidance | CPA |
| :---: | :---: |
| Counting back in multiples of ten and one hundred |  |
| Using known number facts to create derived facts <br> Dienes blocks should be used alongside pictorial and abstract representations when introducing this strategy, encouraging pupils to apply their knowledge of number bonds to add multiples of ten and 100 . | $8-4=4$ <br> leads to <br> $80-40=40$ <br> leads to <br> $800-400=400$ |
| Subtracting tens and ones <br> Pupils must be taught to partition the second number for this strategy as partitioning both numbers can lead to errors if regrouping is required. |  |


| Strategy \& guidance | CPA |
| :---: | :---: |
| Round and adjust (sometimes known as a compensating strategy) <br> Pupils must be taught to round the number that is being subtracted. <br> Pupils will develop a sense of efficiency with this method, beginning to identify when this method is more efficient than subtracting tens and then ones. |  |
| Make ten <br> How pupils choose to apply this strategy is up to them. The focus should always be on efficiency. <br> It relies on an understanding that numbers can be partitioned in different ways in order to subtract to a multiple of ten. <br> Pupils should develop an understanding that the parts can be added in any order. | $42-15=$ |

Mathematics Mastery

| Strategy \& guidance | CPA |
| :---: | :---: |
| Partitioning to subtract without regrouping <br> As in Year 1, the focus is to develop a strong understanding of place value and pupils should always be using concrete manipulatives alongside the pictorial. <br> Formal recording in columns is unnecessary for this mental strategy. It prepares them to subtract with 3-digits when regrouping is required. |  |
| Column method with regrouping <br> The focus for the column method is to develop a strong understanding of place value and concrete manipulatives should be used alongside. <br> Pupils are introduced to calculations that require two instances of regrouping (initially from tens to one and then from hundreds to tens). E.g. 232 -157 and are given plenty of practice using concrete manipulatives and images alongside their formal written methods, ensuring that important steps are not missed in the recording. <br> Caution should be exercised when introducing calculations requiring 'regrouping to regroup' (e.g. 204-137) ensuring ample teacher modelling using concrete manipulatives and images. | $\begin{array}{r} 1417 \\ -\quad 18 \\ \hline 129 \\ \hline \end{array}$hundreds tens ones <br>  $\square$ $\square$ <br> $=$ $\square$ $\ddots$ |

Mathematics Mastery

## National Curriculum objectives linked to multiplication and division

These objectives are explicitly covered through the strategies outlined in this document:

- Recall and use multiplication and division facts for the 2,5 and 10 multiplication tables, including recognising odd and even numbers.
- Recall and use multiplication and division facts for the 3 and 4 multiplication tables (Year 3).
- Show that multiplication of two numbers can be done in any order (commutative) but division of one number by another cannot.

The following objectives should be planned for lessons where new strategies are being introduced and developed:

- Calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication ( $\times$ ), division ( $\div$ ) and equal ( $=$ ) signs.
- Solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods and multiplication and division facts, including problems in context.

Teachers should refer to definitions and guidance on the structures for multiplication and division to provide a range of appropriate real-life contexts for calculations.

Y2 Multiplication


| Strategy \& guidance |
| :--- |
| Arrays to represent |
| multiplication |
| equations |
| Concrete manipulatives <br> and images of familiar <br> objects begin to be <br> organised into arrays <br> and, later, are shown <br> alongside dot arrays. It <br> is important to discuss <br> with pupils how arrays <br> can be useful. |
| Pupils begin to <br> understand <br> multiplication in a more <br> abstract fashion, <br> applying their skip <br> counting skils $t$ identify <br> the multiples of the $2 x, 5 x$ <br> and $10 x$ tables. |
| The relationship between <br> multiplication and <br> division also begins to be <br> demonstrated. |
| Multiplication is <br> commutative |
| Pupils should understand <br> that an array and, later, <br> bar models can represent <br> different equations and <br> that, as multiplication is <br> commutative, the order <br> of the multiplication does <br> not affect the answer. |

Mathematics Mastery

| Strategy \& guidance | CPA |
| :---: | :---: |
| Use of part-partwhole model to establish the inverse relationship between multiplication and division <br> This link should be made explicit from early on, using the language of the part-part-whole model, so that pupils develop an early understanding of the relationship between multiplication and division. Bar models (with Cuisenaire rods) should be used to identify the whole, the value of the parts and the number of parts. <br> It is important to highlight that with multiplication, the parts are of equal value as this is different to how this model is used for addition and subtraction. | There are three equal parts. Each part has a value of three. What is the whole? $9 \div 3=$ $\square$ <br> What multiplication and division equations can you write for each bar model? <br> Prove that the equations are correct using a bead string. $\square$ $\times$ $\square$ $=$ $\square$ $\square$ $\div$ $\square$ $=$ $\square$ |
| Doubling to derive new multiplication facts <br> Pupils learn that known facts from easier multiplication tables can be used to derive facts from related times tables using doubling as a strategy. <br> At this stage they double the $2 \times$ table facts to derive the $4 \times$ table facts. |  |

## Y2 Division

| Strategy \& guidance |  |
| :--- | :--- |
| Division as sharing |  |
| Here, division is shown as |  |
| sharing. |  |
| If we have ten pairs of |  |
| scissors and we share them |  |
| between two pots, there will |  |
| be 5 pairs of scissors in each |  |
| pot. |  |

Mathematics Mastery

\begin{tabular}{|c|c|}
\hline Strategy \& guidance \& CPA \\
\hline \begin{tabular}{l}
Use of part-part-whole model to represent division equations and to emphasise the relationship between division and multiplication \\
Pupils use arrays of concrete manipulatives and images of familiar objects to solve division equations. \\
They begin to use dot arrays to develop a more abstract concept of division. \\
It is important to highlight that with multiplication and division, the parts are of equal value as this is different to how this model is used for addition and subtraction.
\end{tabular} \& \begin{tabular}{l}
\[
\begin{aligned}
\& 15 \div 5=3 \\
\& 15 \div 3=5
\end{aligned}
\]

<br>
Write the division equations that the array represents. <br>
The whole is nine. There are three equal parts. What is the value of each part?
\end{tabular} <br>

\hline
\end{tabular}

# Progression in calculations 

## Year 3

## National Curriculum objectives linked to addition and subtraction

These objectives are explicitly covered through the strategies outlined in this document:

- add and subtract numbers mentally, including:
- a three-digit number and ones
- a three-digit number and tens
- a three-digit number and hundreds
- add and subtract numbers with up to four digits, using formal written methods of columnar addition and subtraction (four digits is Year 4)
- find 10 or 100 more or less than a given number
- find 1000 more or less than a given number (Year 4)
- estimate the answer to a calculation and use inverse operations to check answers

The following objectives should be planned for lessons where new strategies are being introduced and developed:

- solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction


## Teachers should refer to definitions and guidance on the structures for addition and subtraction to provide a range of appropriate real-life contexts for calculations.

## Y3 Addition \& Subtraction

## Strategy \& guidance <br> Add and subtract numbers mentally, including:

- a three-digit number and ones;
- a three-digit number and tens;
- a three-digit number and hundreds

Pupils learn that this is an appropriate strategy when they are able to use known and derived number facts or other mental strategies to complete mental calculations with accuracy.

To begin with, some pupils will prefer to use this strategy only when there is no need to regroup, using number facts within 10 and derivations. More confident pupils might choose from a range of mental strategies that avoid written algorithms, including (but not exhaustively):

- known number facts within 20 ,
- derived number facts,
- 'Make ten',
- round and adjust

See Year 2 guidance for exemplification of these - the use of concrete manipulatives other than Dienes blocks is important in reinforcing the use of these strategies.

It is important that pupils are given plenty of (scaffolded) practice at choosing their own strategies to complete calculations efficiently and accurately. Explicit links need to be made between familiar number facts and the calculations that they can be useful for and pupils need to be encouraged to aim for efficiency.

It is important to model the mental strategy using concrete manipulatives in the first instance and pupils should be able to exemplify their own strategies using manipulatives if required, with numbers appropriate to the unit they are working on (3-digit numbers in Units 1 \& 4; 4-digit numbers in Unit 13). However, pupils should be encouraged to use known facts to derive answers, rather than relying on counting manipulatives or images.

## No regrouping

$345+30 \quad 274-50$
$1128+300 \quad 1312-300$
$326+342 \quad 856-724$


With some regrouping

| $416+25$ | $232-5$ |
| :--- | :--- |
| $383+130$ | $455-216$ |
| $611+194$ | $130-40$ |
| $1482+900$ | $2382-500$ |

## Strategy \& guidance <br> Written column method for calculations that require regrouping with up to 4-digits

Dienes blocks should be used alongside the pictorial representations during direct teaching and can be used by pupils both for support and challenge. Place value counters can also be introduced at this stage.

This work revises and reinforces ideas from Key Stage 1, including the focus on place value - see Year 2 exemplification.

Direct teaching of the columnar method should require at least one element of regrouping, so that pupils are clear about when it is most useful to use it. Asking them 'Can you think of a more efficient method?' will challenge them to apply their number sense / number facts to use efficient mental methods where possible.

As in Year 2, pupils should be given plenty of practice with calculations that require multiple separate instances of regrouping. In Year 3 they become more familiar with calculations that require 'regrouping to regroup'. Understanding must be secured through the considered use of manipulatives and images, combined with careful use of language.

Pupils should be challenged as to whether this is the most efficient method, considering whether mental methods (such as counting on, using known number facts, round and adjust etc.) may be likelier to produce an accurate solution.

Pupils requiring support might develop their confidence in the written method using numbers that require no regrouping.

See Unit materials for extra guidance on this strategy.

## CPA

As for the mental strategies, pupils should be exposed to concrete manipulatives modelling the written calculations and should be able to represent their written work pictorially or with concrete manipulatives when required.
Again, they should be encouraged to calculate with known and derived facts and should not rely on counting images or manipulatives.

$5+6=11$ so | will have 11 ones which | regroup for 1 ten and 1 one.

Regrouping (including multiple separate instances)
$672+136$
734-82
$468+67$
831-76
$275+386$
435-188
'Regrouping to regroup'
204-137
1035-851

| Strategy \& guidance |  |
| :--- | :--- | :--- |
| Find 10, 100 more or less than a given number | $142+100=242$ |
| As pupils become familiar with numbers up to 10oo, |  |
| place value should be emphasised and comparisons |  |
| drawn between adding tens, hundreds (and, in the |  |
| last unit of the Summer term, thousands), including |  |
| use of concrete manipulatives and appropriate |  |
| images. |  |

## National Curriculum objectives linked to multiplication and division

These objectives are explicitly covered through the strategies outlined in this document:

- count from o in multiples of 4, 8,50 and 100
- recall and use multiplication and division facts for the $3,4,6$, and 8 multiplication tables
- write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental methods
- solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which $n$ objects are connected to $m$ objects

Teachers should refer to definitions and guidance on the structures for multiplication and division to provide a range of appropriate real-life contexts for calculations.

## Y3 Multiplication

| Strategy \& guidance |  |
| :--- | :--- |
| Doubling to derive <br> new multiplication <br> facts | $3 \times 3=9$ |
| Pupils continue to make |  |
| use of the idea that facts |  |
| from easier times tables |  |
| can be used to derive |  |
| facts from related times |  |
| tables using doubling as |  |
| a strategy. |  |
| This builds on the |  |
| doubling strategy from |  |
| Year 2. |  | Mathematics Mastery



Mathematics Mastery

| Strategy \& guidance | CPA |
| :---: | :---: |
| Multiplying by 10 and 100 <br> Building on the ten times greater work, pupils use appropriate Dienes blocks and place value counters to multiply 2, 3, 4, 5 and 10 by 10,100 and 1000 . | $\begin{aligned} & 5 \times 1=5 \\ & 5 \times 10=50 \\ & 3 \times 100=300 \end{aligned}$ |
| Using known facts for multiplying by multiples of 10 and 100 <br> Pupils' growing understanding of place value, allows them to make use of known facts to derive multiplications using powers of 10 . <br> It is important to use tables with which they are already familiar (i.e. not 7 or 9 tables in Year 3) |  |



Mathematics Mastery

| Strategy \& guidance | CPA |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Multiplication of 2digit numbers with partitioning (regrouping) <br> Using concrete manipulatives and later moving to using images that represent them, supports pupils' early understanding, leading towards formal written methods in Year 4. <br> Once again, this is a mental strategy, which they may choose to support with informal jottings, including a full grid, as exemplified here. <br> Pupils must be encouraged to make use of their known multiplication facts and their knowledge of place value to calculate, rather than counting manipulatives. | $\times$ <br> 3 <br>  <br> $\times$ |  |  | $\times$ 3 | 10 <br> 30 <br>  | 4 12 -10 80 |  |

Mathematics Mastery

Y3 Division


# Progression in calculations <br> Year 4 

## National curriculum objectives linked to addition and subtraction

These objectives are explicitly covered through the strategies outlined in this document:

- add and subtract numbers with up to four digits, using the formal written methods of columnar addition and subtraction where appropriate
- find 1000 more or less than a given number
- estimate and use inverse operations to check answers to a calculation
N.B. There is no explicit reference to mental calculation strategies in the programmes of study for Year 4 in the national curriculum. However, with an overall aim for fluency, appropriate mental strategies should always be considered before resorting to formal written procedures, with the emphasis on pupils making their own choices from an increasingly sophisticated range of strategies.

The following objectives should be planned for lessons where new strategies are being introduced and developed:

- solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why
- solve simple measure and money problems involving fractions and decimals to two decimal places


## Y4 Addition \& Subtraction

| Strategies \& Guidance | CPA |
| :---: | :---: |
| Count forwards and backwards in steps of 10,100 and 1000 for any number up to 10000 . <br> Pupils should count on and back in steps of ten, one hundred and one thousand from different starting points. These should be practised regularly, ensuring that boundaries where more than one digit changes are included. <br> Count forwards and backwards in tenths and hundredths |  <br> Pay particular attention to boundaries where regrouping happens more than once and so more than one digit changes. $\text { E.g. } 990+10 \text { or } 19.9+0.1$ |
| Using known facts and knowledge of place value to derive facts. <br> Add and subtract multiples of 10 , 100 and 1000 mentally <br> Pupils extend this knowledge to mentally adding and subtracting multiples of 10 , 100 and 1000. Counting in different multiples of 10,100 and 1000 should be incorporated into transition activities and practised regularly. |  |
| Adding and subtracting by partitioning one number and applying known facts. <br> By Year 4 pupils are confident in their place value knowledge and are calculating mentally both with calculations that do not require regrouping and with those that do. | See Y3 guidance on mental addition \& subtraction, remembering that use of concrete manipulatives and images in both teaching and reasoning activities will help to secure understanding and develop mastery. |


| Strategies \& Guidance | CPA |
| :---: | :---: |
| Round and adjust <br> Pupils should recognise that this strategy is useful when adding and subtracting near multiples of ten. They should apply their knowledge of rounding. <br> It is very easy to be confused about how to adjust and so visual representations and logical reasoning are essential to success with this strategy. <br> Build flexibility by completing the same calculation in a different order. | Completing the same calculation but adjusting first: $3527+296=3523+300$ $4523-3997=523+3$ <br> Completing the same calculation but adjusting first: $4523-3997=4526-4000$ |
| Near doubles <br> Pupils should be able to double numbers up to 100 and use this to derive doubles for multiples of ten. These facts can be adjusted to calculate near doubles. | $1600+1598=\text { double } 1600-2$ |

Mathematics Mastery



## Mathematics Mastery

## National Curriculum objectives linked to multiplication and division

## These objectives are explicitly covered through the strategies outlined in this document:

- count from 0 in multiples of $6,7,9,25$ and 1000
- recall and use multiplication and division facts for multiplication tables up to $12 \times 12$
- write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods
- recognise and use factor pairs and commutativity in mental calculations
- use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1 ; dividing by 1 ; multiplying together three numbers
- multiply two-digit and three-digit numbers by a one-digit number using formal written layout
- find the effect of dividing a one- or two-digit number by 10 and 100 , identifying the value of the digits in the answer as ones, tenths and hundredths.


## The following objectives should be planned for lessons where new strategies are being introduced and developed:

- solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as $n$ objects are connected to $m$ objects.

Mathematics
Mastery
Y4 Multiplication




Y4 Division

| Strategies \& Guidance | CPA |
| :---: | :---: |
| Dividing by 10 and 100 <br> When you divide by ten, each part is ten times smaller. The hundreds become tens and the tens become ones. Each digit is in a place that gives it a value that is ten times smaller. <br> When dividing multiples of ten, a place holder is no longer needed so that each digit has a value that is ten times smaller. E.g. $210 \div 10=21$ |  |
| Derived facts <br> Pupils use their growing knowledge of multiplication facts, place value and derived facts to multiply mentally. <br> Understanding of the inverse relationship between multiplication and division allows corresponding division facts to be derived. | $\begin{array}{ll} 210 \div 7=30 & 2100 \div 7=300 \\ 210 \div 3=70 & 2100 \div 3=700 \\ 210 \div 30=7 & 2100 \div 300=7 \\ 210 \div 70=3 & 2100 \div 700=3 \end{array}$ |

Mathematics Mastery

| Strategies \& Guidance | CPA |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Short division of 4-digit numbers by 1-digit numbers | Division as sharing |  |  |  |  |
| Pupils start with dividing 4-digit |  | Th | H | $\uparrow$ | 0 |
| numbers by 2, 3 and 4, where no regrouping is required. Place value |  | $\theta$ | - | 889 |  |
| counters are used simultaneously in a place value chart, to develop conceptual | $3 \longdiv { 3 4 8 6 }$ | - | - | 888 | 8 |
| understanding. |  | - | - | 898 | 8 |
| They progress to calculations that require regrouping in the hundreds or |  |  |  |  |  | tens columns.

Pupils build on their conceptual knowledge of division to become confident with dividing numbers where the tens digit is smaller than the divisor, extending this to any digit being smaller than the divisor.

Exemplification of this method and the language to use are best understood through viewing the tutorial videos found here on the toolkit.

## Division of a one- or two-digit

 number by 10 and 100, identifying the value of the digits in the answer as ones, tenths and hundredthsWhen you divide by ten, each part is ten times smaller. The tens become ones and the ones become tenths. Each digit is in a place that gives it a value that is ten times smaller.

$24 \div 100=0.24$


## Progression in calculations

## Year 5 + Year 6

Year 5 and Year 6 are together because the calculation strategies used are broadly similar, with Year 6 using larger and smaller numbers. Any differences for Year 6 are
highlighted in red.

## National Curriculum objectives linked to integer addition and subtraction

These objectives are explicitly covered through the strategies outlined in this document:

- add and subtract numbers mentally with increasingly large numbers
- add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction)
- use negative numbers in context, and calculate intervals across zero
- perform mental calculations, including with mixed operations and large numbers
- use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy

The following objectives should be planned for lessons where new strategies are being introduced and developed:

- use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy
- solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why
- solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign.
$\mathbf{Y}_{5}$ and Y6 Addition \& Subtraction

| Strategies \& Guidance | CPA |
| :---: | :---: |
| Count forwards or backwards in steps of powers of 10 for any given number up to 1000000 <br> Skip counting forwards and backwards in steps of powers of 10 (i.e. $10,100,1000,10000$ and 100 OOO ) should be incorporated into transition activities and practised regularly. <br> In Year 5 pupils work with numbers up to 1 ooo ooo as well as tenths, hundredths and thousandths. <br> In Year 6 pupils work with numbers up to 10 o00 000 . | Support with place value counters on a place value chart, repeatedly adding the same counter and regrouping as needed. <br> Counting sticks and number lines: <br> $97009800 \quad 9900$ <br> Pay particular attention to boundaries where regrouping happens more than once and so more than one digit changes. e.g. $9900+100=10000$ or $99000+1000=100000$ |
| Using known facts and understanding of place value to derive <br> Using the following language makes the logic explicit: I know three ones plus four ones is equal to seven ones. Therefore, three ten thousands plus four ten thousands is equal to seven ten thousands. <br> In Year 5 extend to multiples of 10 ooo and 100 ooo as well as tenths, hundredths and thousandths. <br> In Year 6 extend to multiples of one million. <br> These derived facts should be used to estimate and check answers to calculations. | $\begin{aligned} & 20000+40000=60000 \\ & 40000+20000=60000 \\ & 60000-40000=20000 \\ & 60000-20000=40000 \end{aligned}$ $\begin{aligned} & 0.6=0.2+0.4 \\ & 0.6=0.4+0.2 \\ & 0.2=0.6-0.4 \\ & 0.4=0.6-0.2 \end{aligned}$ |

## Strategies \& Guidance <br> Partitioning one number and applying known facts to <br> add.

Pupils can use this strategy mentally or with jottings as needed.

Pupils should be aware of the range of choices available when deciding how to partition the number that is to be added.

They should be encouraged to count on from the number of greater value as this will be more efficient. However, they should have an understanding of the commutative law of addition, that the parts can be added in any order.

Pupils have experience with these strategies with smaller numbers from previous years and so the focus should be on developing flexibility and exploring efficiency.

Partitioning into place value amounts (canonical partitioning):
$4650+7326=7326+4000+600+50$


With place value counters, represent the larger number and then add each place value part of the other number. The image above shows the thousands being added.

Represent pictorially with an empty numberline:


Partitioning in different ways (non-canonical partitioning):
Extend the 'Make ten' strategy (see guidance in Y1 or Y2) to count on to a multiple of 10.
$6785+2325=6785+15+200+2110$


The strategy can be used with decimal numbers, Make one:
$14.7+3.6=14.7+0.3+3.3=15+3.3$


| Strategies \& Guidance |
| :--- |
| Subtraction by partitioning <br> and applying known facts. |
| Pupils can use this strategy <br> mentally or with jottings as <br> needed. |
| Pupils should be aware of the |
| range of choices available when |
| deciding how to partition the |
| number that is to be subtracted. |$|$| Pupils have experience with |
| :--- |
| these strategies with smaller |
| numbers from previous years |
| and so the focus should be on |
| developing flexibility and |
| exploring efficiency. |

Partitioning into place value amounts (canonical partitioning): $75221-14300=75221-10000-4000-300$


Represent pictorially with a number line, starting on the right and having the arrows jump to the left:


Develop understanding that the parts can be subtracted in any order and the result will be the same:


Partitioning in different ways (non-canonical partitioning):
Extend the 'Make ten' strategy (see guidance in Y1 or Y2) to count back to a multiple of 10 .


| Strategies \& Guidance | CPA |
| :---: | :---: |
| Calculate difference by "counting back" <br> It is interesting to note that finding the difference is reversible. For example, the difference between 5 and 2 is the same as the difference between 2 and 5. This is not the case for other subtraction concepts. | 75 221-14300 <br> Place the numbers either end of a numberline and work out the difference between them. Select efficient jumps. <br> Finding the difference is efficient when the numbers are close to each other: $9012-8976$ |
| Calculate difference by "counting on" <br> Addition strategies can be used to find difference. | $75221-14300$ <br> Finding the difference is efficient when the numbers are close to each other $9012-8976$ |


| Strategies \& Guidance | CPA |
| :---: | :---: |
| Round and adjust <br> Addition and subtraction using compensation <br> Pupils should recognise that this strategy is useful when adding and subtracting near multiples of ten. They should apply their knowledge of rounding. <br> It is very easy to be confused about how to adjust and so visual representations and logical reasoning are essential to success with this strategy. | Addition <br> $54128+9987=54128+10000-13=64128-13$ <br> Pupils should realise that they can adjust first: $54128+9987=54128-13+10000=54115+10000$ <br> Subtraction $78051-9992=78051-10000+8=68051+8$ <br> Pupils should realise that they can adjust first: <br> $78051-4960=78051+40-5000=78692-5000$ |
| Near doubles <br> Pupils should be able to double numbers up to 100 and use this to derive doubles for multiples of ten as well as decimal numbers. These facts can be adjusted to calculate near doubles. | $\begin{aligned} & 160+170=\text { double } 150+10+20 \\ & 160+170=\text { double } 160+10 \text { or } 160+170=\text { double } 170-10 \\ & 2.5+2.6=\text { double } 2.5+0.1 \end{aligned}$ |


| Strategies \& Guidance |
| :--- |
| Partition both numbers and <br> combine the parts |
| Pupils should be secure with this |
| method for numbers up to 10 |
| ooo, using place value counte |
| or Dienes to show conceptual |
| understanding. |
| If multiple regroupings are |
| required, then pupils should |
| consider using the column |
| method. |

In Year 5, pupils are expected to be able to use formal written methods to add whole numbers with more than four digits as well as working with numbers with up to three decimal places.

Pupils should think about whether this is the most efficient method, considering if mental methods would be more effective.

Continue to use concrete manipulatives alongside the formal method.

When adding decimal numbers with a different number of decimal places, in order to avoid calculation errors, pupils should be encouraged to insert zeros so that there is a digit in every row. This is not necessary for calculation and these zeros are not place holders as the value of the other digits is not changed by it being placed.

Exemplification of this method and the language to use are best understood through viewing the tutorial videos found here on the toolkit.


Pupils should be aware that the parts can be added in any order.
For this method start with the digit of least value because if regrouping happens it will affect the digits of greater value.


Combine the counters in each column and regroup as needed:


Decimal numbers:


## Strategies \& Guidance <br> Written column methods for subtraction

In Year 5, pupils are expected to be able to use formal written methods to subtract whole numbers with more than four digits as well as working with numbers with up to three decimal places.

Pupils should be given plenty of practice with calculations that require multiple separate instances of regrouping.

In Year 3 and 4 they become more familiar with calculations that require 'regrouping to regroup'. Understanding must be secured through the considered use of manipulatives and images, combined with careful use of language.

Pupils should think about if this is the most efficient method, considering whether mental strategies (such as counting on, using known number facts, compensation etc.) may be likelier to produce an accurate solution.

Exemplification of this method and the language to use are best understood through viewing the tutorial videos found here on the toolkit.


The term regrouping should be the language used. You can use the terms 'exchange' with subtraction but it needs careful consideration.

You can regroup 62 as 50 and 12 ( 5 tens and 12 ones) instead of 60 and 2 ( 6 tens and 12 ones).

Or you can 'exchange' one of the tens for 10 ones resulting in 5 tens and 12 ones.

If you have exchanged, then the number has been regrouped.

## Progression in calculations

## Year 5 + Year 6

## National Curriculum objectives linked to multiplication and division

## These objectives are explicitly covered through the strategies outlined in this document:

- multiply and divide whole numbers by 10,100 and 1000
- multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers
- multiply and divide numbers mentally drawing upon known facts
- divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context
- multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication
- divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context
- divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context
- multiply one-digit numbers with up to two decimal places by whole numbers
- use written division methods in cases where the answer has up to two decimal places


## The following objectives should be planned for lessons where new strategies are being introduced and developed:

- solve problems involving multiplication and division including using their knowledge of factors and multiples, squares and cubes
- solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign
- use their knowledge of the order of operations to carry out calculations involving the four operations
- solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why
- solve problems involving addition, subtraction, multiplication and division
- solve problems involving the relative sizes of two quantities where missing values can be found by using integer multiplication and division facts.

Mathematics
Mastery
Y5 and Y6 Multiplication

| Strategies \& Guidance | CPA <br> When you multiply by ten, each part is ten times greater. The ones become tens, the tens become hundreds, etc. <br> When multiplying whole numbers, a zero holds a place so that each digit has a value that is ten times greater. $102.14 \times 10=1021.4$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Multiply and divide whole numbers and those involving decimals by 10 , 100 and 1000 <br> Avoid saying that you "add a zero" when multiplying by ten and instead use the language of place holder. <br> Use place value counters and charts to visualise and then notice what happens to the digits. |  |  |  |  |  |
|  | Thousands | Hundeds | Tens | Ones . | hundradtrs |
|  |  |  |  | (1) | (0.1) 01.1 |
|  |  |  |  |  | $\sqrt{2}$ |
|  | When you hundreds place that When divid so that eac E.g. $210 \div$ $210.3 \div 10$ | ivide by t come ten ives it a va <br> ng multipl digit has $0=21$ <br> 21.03 | , each pa and the e that is of ten, value tha | is ten times sm ns become one n times smaller. <br> place holder is $n$ is ten times sm | ler. The Each digit is in a longer needed er. |
|  | Hundreds | Tens |  | - tentrs | hundreaths |
|  | (100) |  |  |  |  |
|  |  | (10) |  | - |  |

Mathematics
Mastery


These are the multiplication facts pupils should be able to derive from a known fact

| 2100000 |  | $700000 \times 3$ | $70000 \times 30$ | $7000 \times 300$ | $700 \times 3000$ | $70 \times 30000$ | $7 \times 300000$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 210000 |  | $70000 \times 3$ | $7000 \times 30$ | $700 \times 300$ | $70 \times 3000$ | $7 \times 30000$ |  |
| 21000 |  | $7000 \times 3$ | $700 \times 30$ | $70 \times 300$ | $7 \times 3000$ |  |  |
| 2100 |  | $700 \times 3$ | $70 \times 30$ | $7 \times 300$ |  |  |  |
| 210 |  | $70 \times 3$ | $7 \times 30$ |  |  |  |  |
| 21 | $=$ | $7 \times 3$ |  |  |  |  |  |
| 2.1 |  | $0.7 \times 3$ | $7 \times 0.3$ |  |  |  |  |
| 0.21 |  | $0.07 \times 3$ | $0.7 \times 0.3$ | $7 \times 0.03$ |  |  |  |
| 0.021 |  | $0.007 \times 3$ | $0.07 \times 0.3$ | $0.7 \times 0.03$ | $7 \times 0.003$ |  |  |



Mathematics Mastery


| Strategies \& Guidance | CPA |
| :---: | :---: |
| Formal written method of short multiplication <br> Conceptual understanding is supported by the use of place value counters, both during teacher demonstrations and during their own practice. <br> Exemplification of this method and the language to use are best understood through viewing the tutorial videos found here on the toolkit. |  |
| Multiplying by a 2-digit number <br> Formal written method of long multiplication <br> In Year 6 pupils are extended from multiplication by a 1digit number to multiplication by a 2-digit number. <br> Extend the place value chart model used in Year 4, using an additional row on the place value chart. <br> Extend understanding of the distrubitive law to develop conceptual understanding of the two rows of the formal written method. <br> Dienes blocks can be used to construct area models to represent this. |  |

Mathematics
Mastery
Y5 and Y6 Division

| Strategies \& Guidance | CPA |
| :---: | :---: |
| Deriving facts from known facts | $6 \div 2=3$ $6 \div 3=2$ |
| Pupils use their growing knowledge of multiplication facts, place value and derived facts to multiply mentally. | $\begin{aligned} & 60 \div 2=30 \\ & 60 \div 30=2 \end{aligned}$ |
| Understanding of the inverse relationship between multiplication and division allows corresponding division facts to be derived. |  |
| Using knowledge of multiples to divide <br> Using an area model to partition the whole into multiples of the divisor (the number you are dividing by). | $112 \div 8=80 \div 8+32 \div 8$ $1260 \div 6=1200 \div 6+60 \div 6$ |



Mathematics
Mastery


Mathematics Mastery

| Strategies \& Guidance | CPA |
| :---: | :---: |
| Long division <br> Dividing a 4-digit number by a 2-digit number <br> Follow the language structures of the short division strategy. Instead of recording the regrouped amounts as small digits the numbers are written out below. This can be easier to work with when dividing by larger numbers. <br> If dividing by a number outside of their known facts, pupils should start by recording some multiples of that number to scaffold. |  |

Mathematics

## Mathematics Mastery vocabulary list

This document highlights the vocabulary introduced throughout the primary curriculum - from Reception to Year 6.

The vocabulary listed here is vocabulary that pupils are expected to use and understand on a daily basis within that year group, though the definitions are written for teacher reference and would not necessarily be shared with children as they stand. The vocabulary listed is cumulative and builds on the vocabulary previously introduced. Teachers should also consult with the Mathematics Mastery Primary Glossary.
This is a working document and will be updated as required.

| Reception | Definition | Example |
| :--- | :--- | :--- |
| Above | Used to describe a higher position <br> than another object. | The Maths Meetings board is above the <br> sink. |
| Add | Carry out the process of addition. | I can add two numbers together to find a <br> total. |
| Addition | The operation to combine at least <br> two numbers or quantities to form a a <br> further number or quantity, the sum <br> or total. Addition is the inverse <br> operation to subtraction. | Three plus seven is equal to ten. This is <br> an addition equation. |
| Altogether | In total. | That will be £2 altogether please. <br> A measuring tool used to weigh <br> objects. It has two dishes hanging <br> on a bar. Both dishes will be level <br> when the contents weigh the same. <br> Also, as a verb, indicates <br> equivalence and equality. |
| The objects in the balance are unequal <br> in weight because the dish on the right <br> side is lower down that the dish on the <br> left side. <br> The two objects balance which means <br> they have the same mass. |  |  |
| Before | In front of or prior to. | The number '3' comes before '5' on the <br> number line. |
| Below | Used to describe a lower position <br> than another object. | The sink is below the Maths Meetings <br> board. |
| Between | Indicates a position in relation to <br> two other places or objects on <br> either side. | The teacher is standing between two <br> tables. |
| Capacity | The amount of liquid a container <br> can hold. | This cup is full to capacity because it <br> cannot hold any more water. |
| Circle | The name of a 2-D shape. A circle <br> has a curved side. | Cor |
| Cost | A tool used to measure time. | The clock shows us that the time is now <br> 2 o'clock. |
| Compare | Look for similarities and/or <br> differences between at least two <br> objects or sets. | I can compare these two sets - this set <br> has more. |
| good or service. |  |  |
| teet. The correct mathematical |  |  |$\quad$| The table has four corners (vertices). |
| :--- |
| Corex vertices). |

Mathematics Mastery

Mathematics
Mastery

| Count | Assigning one number name to each of a set of objects to determine how many there are. | I counted the children in the group there are four so we will need four pencils. |
| :---: | :---: | :---: |
| Cube | A 3-D shape with six identical square faces. |  |
| Cuboid | A 3-D shape with six rectangular faces. |  |
| Curved surface | A non-plane surface of a 3-D shape. Both cones and cylinders have curved surfaces. | The cone has a curved surface. |
| Cylinder | A 3-D shape with two circular faces joined by a curved surface. | 0 |
| 2-D | Abbreviation for two-dimensional. A figure is two-dimensional if it lies on a plane. | A square is a 2-D shape. |
| 3-D | Abbreviation for three-dimensional. A solid is three-dimensional and occupies space. | A cylinder is a 3-D shape. |
| Describe | To express mathematical features, qualities and details in words. | Can you describe the properties of a cube? |
| Difference | The numerical difference between two numbers or sets of objects. It is found by comparing the quantity of one set of objects with another. | The difference between ten and six is four. |
| Direction | The orientation of a line in space. | Which direction should we jump forwards or backwards? |
| Distance | A measure between two points or things. | The distance between my house and the school is longer than that between the school and the train station. |
| Double | To multiply by two or add a value to itself. | Ten is double five. |
| Edge | A line segment joining two vertices of a plane figure (2-D shape) and the intersection of two plane faces (in a 3-D shape). | A triangle has three edges and a cube has 12 edges. |
| Empty | Containing nothing. Most commonly used in the context of measures. | There is no more water left in the jug - it is empty. |
| Equal | Indicates equivalence between two values and can be expressed with the symbol ' $x$ '. The symbol is read as 'is equal to' which means the same as. Expressions on either side of the symbol have the same value. | My sets are equal because there are four bears in this set and there are four bears in this set. |
| Face | One of the plane surfaces of a solid shape. | A cube has six faces. |

Mathematics Mastery

Mathematics
Mastery

| Fewer | A lesser amount - used when counting discrete objects, i.e. countable objects such as, pens, teddies, counters, etc. | There are fewer buttons on my coat than yours. |
| :---: | :---: | :---: |
| First | Comes before all others in time or position. | First I brush my teeth. Then I go to bed. |
| Flat | A level surface. | The table has a flat rectangular surface. |
| Full | Contains/holds as much or as many as possible; has no empty space. | The juice carton is not full because I drank some. |
| Group | To make equal size groups. This is one model for division. | I will group the crayons equally so that each person gets two. |
| Half | One of two equal parts of a shape, quantity or object. | I have shared the dolls into two equal groups - I have half and you have half. |
| Intersection of sets | Where the two subsets overlap in a Venn diagram. Objects or values which belong to both subsets are placed here. | The number 4 belongs in the intersection because it is even and less than 5. |
| Last | Comes after all others in time or order. | Rory is the last person in the line. |
| Length | A linear measurement. | The length of my snake is shorter than yours. |
| Less | A smaller amount or not as much. | I have 15p and you have 7p. you have less money than me. |
| Line | A set of adjacent points that has length but no width. | I have drawn a line matching the number four with the four ducks. |
| Long | An adjective used to describe length. | I have a long piece of string. |
| Mass | A measure relating to the amount of matter within a given object. | The mass of the school bag is greater than the mass of the book. |
| Measure | To find the size of something in a given unit. | How might we measure how much flour we need to bake a cake? |
| Minus | A name for the symbol ' - ', which denotes the operation of subtraction. | Three minus one is equal to two. |
| More | A greater amount. | I have six apples and you have two. I have more. |
| Next | Comes immediately after the present one in order. | The next shape in my pattern is a square. |
| Number bond | A pair of numbers with a given total. | Five and four make a number bond to nine. |
| Number line | A linear, continuous representation of number. Each number occupies a point on the line, and there is an equal interval between each number. | This number line starts at zero and ends at ten. |
| Number track | A linear, discrete representation of number. Each number is positioned in a square on the track. | I can count from one to ten, moving a counter along this number track. |
| Order | Describes the placement of items according to given criteria or in a pattern. <br> As a verb, to place items according to given criteria or in a pattern. | I have ordered the bears from smallest to biggest. |

Mathematics
Mastery

| Pair | A set of two things used together. | Socks come in a pair - one for each foot. |
| :---: | :---: | :---: |
| Pattern | A systematic arrangement of numbers, shapes or other elements according to a rule. | The pattern is red, blue, red, blue, red blue. |
| Plus | The word representing the operation of addition. It is also the name for the symbol ' + ' | Five apples plus two apples are equal to seven apples. |
| Rectangle | A quadrilateral with four right angles. |  |
| Second | 1. A unit of time. <br> 2. An ordinal number. | Mohsin is second in the line today. |
| Sequence | A series of numbers or other elements which follow a rule. | The number 3 is next in the sequence because each number is one less than the one before. |
| Set | A defined group of objects, numbers or other elements. | I have placed all the purple counters in this set because they are all the same colour. |
| Share | To distribute fairly between a given number of recipients. This is one model for division. | I will share the crayons equally between the people at the table. |
| Short | An adjective used to describe length. | This string will not reach to the door. It is too short. |
| Side | A straight line that forms part of the boundary of a shape. | This shape has four straight sides. |
| Size | An element's overall dimensions or magnitude. | The size of my shoe is smaller than my teacher's. |
| Sort | To organise a set of elements into specified categories. | I will sort these objects based on their size. |
| Square | A quadrilateral with four equal length sides and four right angles. |  |
| Straight | A line or movement uniform in direction, without bends or curves. | The walls of the school are straight. |
| Subtract | Carry out the process of subtraction. | Nine subtract three is equal to six. |
| Subtraction | The inverse operation to addition. | We are taking some away so it is a subtraction question. |
| Sum | The result of one or more additions. | The sum of five and three is eight. |
| Surface | An outer boundary of a 3-D object. | This cone has a curved surface. |
| Take away | Used in the reduction structure of subtraction. To remove a number of items from a set. | He ate three of the sweets so we need to take away three counters. |
| Tall | Measuring a specific distance from top to bottom. | Our class teacher is not as tall as our head teacher. |
| Time | Related to duration. Measured in seconds, minutes, hours, days, weeks, months, years etc. | After lunch it will be time for P.E. |
| Total | The sum found by adding. | There are a total of five people at this table. |
| Triangle | A polygon with three sides. |  |

## $\pm \times$ - <br> Mathematics <br> Mastery

| Venn diagram | Two or more circles which <br> represent given sets and intersect <br> according these. |  |
| :--- | :--- | :--- |
| Vertex (pl. <br> vertices) | The point at which two or more <br> lines intersect. | This shape has five vertices. |
| Weight | The force exerted on an object by <br> gravity. Weight therefore changes <br> with a change in gravitational force. <br> Used interchangeably with mass <br> until KS2. | The weight of this book is heavier than <br> the pencil. |
| Zero | The number before one. It is <br> neither positive nor negative. | Zero comes before one on the number <br> track. |


| Year 1 | Definition | A clock with a face and hands. |  |
| :--- | :--- | :--- | :--- |
| Analogue clock |  | Movement in the opposite direction <br> to the motion of the hands of a <br> clock. | The number is not exact but it is <br> close. |
| Anticlockwise |  |  |  |
| An arrangement of counters or |  |  |  |
| used to represent multiplication |  |  |  |
| and division |  |  |  |, | The pre-cursor to the bar graph, |
| :--- |
| this representation of data has an |
| x- and y-axis and one block |
| represents one item. Each block is |
| adjoined to the adjacent block. |


| Cone | A 3-D shape with one circular plane face, which tapers to an apex. |  |
| :---: | :---: | :---: |
| Continuous surface | An outer boundary of a 3-D object which is uninterrupted by any plane surfaces. | A sphere has a continuous surface. |
| Data | Quantitative information which has been counted or measured. | This block graph shows us data for the colour of the cars in the car park. |
| Decreasing | Becoming smaller in value. Used in relation to number sequences. | $15,14,13,12$. This number pattern is decreasing by one each time. |
| Diagram | An illustration, drawing or representation. | I will draw a diagram to show how I programed my floor toy to move. |
| Digit | One of the ten Arabic numerals 0 to 9 , from which we compose numbers. | The number 54 has the digit five in the tens column and the digit four in the ones. The digit five has a value of fifty. |
| Divide | To share or group into equal parts. | I can divide 12 by three using grouping or sharing. |
| Estimate | An appropriately accurate guess, depending on the context and numbers involved. | I estimate there are eight cubes in the cup because it looks about double four but fewer than ten. |
| Even number | A number with a $0,2,4,6$ or 8 in the ones and therefore exactly divisible by two. | 32 is an even number. |
| Facts | Related to the four operations (,+- , $\times, \div$ ). Pupils should be supported in achieving fluency, i.e. very fast recall, in these facts. These then become known facts. | Number bonds to and within 10 and 20 are facts, e.g. $3+7=10$. |
| Fraction | 1. A part of a whole number, quantity or shape. <br> 2. Expressing a division relationship between two integers in the form $\frac{a}{b}$. | I have shared my sweets into four equal parts. Everyone will get a fraction of the whole quantity of sweets. One group is a quarter of the whole. |
| Half turn | A 180 degree rotation, i.e. $\frac{1}{2}$ of a 360 degree or 'full' turn. |  |
| Hour | A unit of time. | There are 24 hours in one day. |
| Increasing | Becoming greater in value. Used in relation to number sequences. | $2,4,6,8$. This number pattern is increasing by two each time. |
| Kilogram | A standard unit of mass, equal to 1000 grams. | The book has a mass of two kilograms. |
| Known fact | A number fact which has been committed to memory (or very fast recall) and can be applied fluently to various calculation strategies. | When I use the 'Make ten' strategy to add, I use known facts to partition the number I'm adding. |
| Left | Indicating the position or direction. | Make a quarter turn left and walk forward three steps. |
| Litre | A standard unit of volume, equal to 1000 millilitres. | The capacity of the jug is about half a litre. |

Mathematics Mastery

Mathematics
Mastery

| Mental calculation | A calculation performed without using a formal written strategy. Simple jottings may aid a mental calculation. | 14 plus 5 is equal to 19 . I completed this using a mental calculation and deriving facts because I know that four plus five is equal to nine. |
| :---: | :---: | :---: |
| Metre | A standard unit of measure, equal to 100 centimetres. | I estimate that the table is about a metre tall. |
| Minute | A unit of time. | We will have lunch in five minutes. |
| Oblong | A quadrilateral with two pairs of parallel sides of equal length. |  |
| Odd number | An integer which is not divisible by two without a remainder. | All numbers which end in 1, 3, 5, 7 and 9 are odd numbers. |
| Partition | To split a number into two or more parts. | The number 23 can be canonically partitioned (by place value) into 20 and 3 , or non-canonically partitioned in many different ways, including 18 and 5 , 17 and 6, etc. |
| Place value | A system for writing numbers, in which the value of a digit is defined by its position within the number. | In the number 452 written in base ten, the digit four has a value of 400 , the five has a value of 50 and the two has a value of two. |
| Position | Location, expressed either descriptively using positional prepositions, or specified by coordinates. | The book is on the table. The clock is hanging above the board. |
| Pound (sterling) | The official currency of the United Kingdom. | Pounds sterling are written using the $£$ symbol. There are 100 pence in one pound sterling. |
| Property | Any attribute. | A property of a triangle is that it has three straight sides and three vertices, the sum of whose angles is 180 degrees. |
| Pyramid | A 3-D shape with a polygonal base and otherwise triangular faces, which form edges with the base, and which meet at an apex. |  |
| Quantity | An amount, in some cases given a numerical value. | A quantity of apples is placed on the left-hand side of the balance. How many kilogram masses will we need to place on the right to balance the apples? |
| Quarter | One of four equal parts of a whole, quantity or object. | I have shared the eight conkers into four equal groups - I have two conkers, which is one quarter of the whole. |
| Quarter turn | A 90 -degree rotation, i.e. $\frac{1}{4}$ of a 360 degree 'full' turn. |  |
| Repeated addition | A structure of multiplication where equal parts are added to make a whole. | I can show $4 \times 5$ as repeated addition: $4+4+4+4+4$. |


| Repeated subtraction | A structure of division, where equal parts are subtracted and the number of equal parts summed to calculate a quotient. | I can use repeated subtraction to calculate 20 divided by four: 20-4-4-4-4-4. |
| :---: | :---: | :---: |
| Represent | To express or show a mathematical concept using words, numerals and symbols, pictures, diagrams, or concrete manipulatives. | I have used three blue cubes to represent the three oranges in the question. I used a part-whole model to represent the addition question. |
| Right | Indicating the position or direction. | The picture is on the right-hand side of the board. |
| Rule | A consistent pattern which allows generalisation. Awareness of a rule allows a pupil to continue a sequence or generate a related sequence. | $2,5,8,11,14 \ldots$ <br> The rule is that each number is three greater than the previous number. Therefore, the next number in this sequence will be 17. |
| Scales | An object used to measure mass. | The scales showed that the banana had a greater mass than the apple. |
| Sign | Synonymous with symbol in its mathematical context, e.g.,,$+- \times$, $\div=$. | $20 \square 5=4$. What is the missing sign? |
| Standard unit | A uniform measure, agreed upon as standard. | Standard units of mass include grams and kilograms. <br> Standard units of length include centimetres, metres and kilometres. Standard units of volume and capacity include millilitres and litres. |
| Sphere | A 3-D shape with a continuous surface, which is at all points equidistant from its centre. It has an infinite number of flat faces and straight edges. | A bowling ball is a sphere. |
| Symbol | Synonymous with sign in its mathematical context, e.g.,,$+- \times$, $\div=$. | $20 \square 5=4$. What is the missing symbol? |
| Table | A structure organised into columns and rows, in which data can be recorded. | The information for Thursday is not yet complete on the table because it is only Wednesday. |
| Turn | Rotation (see half and quarter tum). | A whole turn is 360 degrees. A half tum is 180 degrees. A quarter turn is 90 degrees. |
| Unit | 1. An element considered as a single entity. Ten single cubes can be grouped together to make a unit of ten. <br> 2. A unit of measure, which can be standard or nonstandard. | I regrouped ten ones for one unit of ten. <br> Unifix cubes can be used as units of measure, but these are not standard units. |
| Volume | A quantity or amount of any substance and the 3-D space it fills. | The bottle contains a volume of one litre but its capacity is two litres. The bottle is half full. |

Mathematics
Mastery

| Year 2 | Definition | Example |
| :---: | :---: | :---: |
| Angle | The amount of tum, measured in degrees. | The angle is 60 degrees. |
| Calculate | To compute or work out mathematically. | Can you calculate the answer to $13+4$ ? |
| Centimetre | A metric unit of length. | The book is 15 centimetres long. |
| Column | A vertical arrangement of numbers or objects. | 23 has two tens - I will place them into the tens column. |
| Commutative | A property of addition and multiplication. It does not matter in which order the addends or factors are added or multiplied; the result will be the same. | $\begin{aligned} & 4+6=10 \\ & 6+4=10 \end{aligned}$ <br> This demonstrates that addition is commutative. <br> Arrays demonstrate the commutativity of multiplication, i.e. $3 \times 4=4 \times 3$ |
| Consecutive | Following in order. | $2,3,4,5,6$ are consecutive numbers. 3 , 6 and 9 are consecutive multiples of 3 . |
| Denominator | The number written below the vinculum in a fraction. In a measure context, it indicates the number of equal parts into which the whole is divided. In a division context, it is the divisor. | In the fraction one quarter, four is the denominator. |
| Division | The process of partitioning a whole into equal parts. | 12 divided by 3 is equal to 4 . |
| Efficient | Well-organised. Choosing an efficient computation strategy requires consideration of the numbers involved and will normally utilise 'known facts'. | I will use my number bonds knowledge to calculate $22+7$ efficiently. I know that 2 +7 is equal to 9 , so the answer is 29 . That's more efficient that counting on seven. |
| Frequency | The number of times something occurs within a data set. | 4 pupils have brown hair. The frequency of brown hair is 4 . |
| Gram | A metric unit of mass. | The pencil weighs 20 grams. |
| Heptagon | A polygon with seven sides and seven angles. | $\sim$ |
| Hexagon | A polygon with six sides and six angles. |  |
| Inverse operations | Opposite operations that 'undo' each other. | Addition and subtraction are inverse operations. |
| Millilitre | A metric unit of capacity/volume. | The can of fizzy drink has a capacity of 330 millilitres. |
| Multiple | The result of multiplying a number by an integer, for example, 12 is a multiple of 3 and 4 because $3 \times 4=$ 12. | 36 is a multiple of three because three multiplied by 12 is equal to 36 . It is also a multiple of 12 for the same reason (and $1,2,4,6,9,18$ and 36 ). |
| Multiplication | One of the four mathematical operations. Multiplication can be understood as repeated addition or scaling (introduced in Year 3). | The multiplication symbol is $\times$. |
| Multiply | To increase a quantity by a given scale factor. | I can multiply 3 by 4 which is equal to 12. |

Mathematics
Mastery

| Near double | When two numbers involved in an addition are close in value, such as $23+22$. The numbers can be treated as exact doubles, followed by compensating. | To calculate $23+22$, I can use the near double strategy. I can double 22 and then add one more. |
| :---: | :---: | :---: |
| Non-unit fraction | A fraction with a numerator greater than one. | Two thirds is a non-unit fraction. |
| Numerator | The number written above the vinculum in a fraction. In a measure context, it indicates the specified number of parts out of the whole. In a division context, it is the dividend. | In the fraction one quarter, one is the numerator. |
| Octagon | A polygon with eight sides and eight angles. |  |
| Operation | A mathematical process. The four mathematical operations are addition, subtraction, multiplication and division. | $4+2=6$. The operation is addition. |
| Pentagon | A polygon with five sides and five angles. |  |
| Pictogram | A representation of data using pictures or symbols. | Countries people visited |
| Quadrilateral | A 2D shape with four sides and four angles. which add up to 360 degrees. |  |
| Relationship | The way in which two or more things are connected. | The relationship between addition and subtraction is that they are the inverse of each other. |
| Right angle | An angle of 90 degrees. | A square has four right angles. |
| Rotation | The act of rotating about an axis/centre. | I will rotate the square 90 degrees clockwise. |
| Scale | Equally spaced markings on a measuring device which can be read to quantify a measurement. | Using the scale on the ruler, the book measures 15 cm . |
| Symmetry | A shape is symmetrical when it fits exactly onto itself when folded in half. | This triangle has gne line of symmetry. |
| Tally | A form of counting. Each tally is a vertical mark. After the fourth vertical mark, a fifth | Four children have black hair, I will record this as four tallies. |

Mathematics

Mathematics
Mastery

|  | horizontal/diagonal mark is drawn <br> to create a group of five. |  |
| :--- | :--- | :--- |
| Temperature | The measure of heat. | Outside has a temperature of 15 <br> degrees Celsius. |
| Unit fraction | A fraction with a numerator of one. | One-third is a unit fraction. |
| Vinculum | A horizontal line that separates the <br> numerator and the denominator in <br> a fraction. | $\frac{1}{4} \longleftarrow$ vinculum |


| Year 3 | Definition | Example |
| :--- | :--- | :--- |
| Acute angle | An angle that is smaller than a <br> right angle. | It is smaller than my right angle checker <br> so this must be an acute angle. |
| Axis (plural: axes) | A real or imaginary reference <br> line. The y-axis (vertical) and x- <br> axis (horizontal) on charts and <br> graphs are used to show the <br> measuring scale or labels for the <br> variables. | The y-axis on this bar graph shows you <br> how many pupils preferred each colour. |
| Bar graph | A representation of data in <br> which the frequencies are <br> represented by the height or <br> length of the bars. | This bar graph shows us the preferred <br> colours of the pupils in our Year 3 class. |
| Columnar <br> addition/subtraction | The formal written algorithms for <br> addition and subtraction that are <br> exemplified in Mathematics | Solve the following calculations by using <br> Ape appropriate method of columnar <br> addition or subtraction. <br> curriculum. of the 2014 national |
| A number, that when multiplied <br> with one or more other factors, <br> makes a given number. | The number six has four factors: 1, 2, 3 <br> and 6. |  |
| Formal written <br> methods | Exemplified in Mathematics <br> Appendix 1 (see above). As well <br> as including columnar addition <br> and subtraction, these also <br> consist of written algorithms for <br> multiplication and division. | Pupils should only use formal written <br> methods for calculations that cannot be <br> efficiently calculated using mental <br> strategies (with or without jottings). |
| Horizontal | Horizontal refers to planes and <br> line segments that are parallel to <br> the horizon. | The x-axis on a graph should be <br> horizontal. |
| Millimetre | In geometry, irregular is a term <br> used to describe shapes that <br> are not regular (see below). | The sides and the angles of this <br> pentagon are not all equal so the <br> pentagon is irregular. <br> A metric unit measure of length <br> that is equal to one thousand <br> metres. |
| A metric unit measure of length <br> that is equal to one thousandth <br> of one metre. | The length of Philippa's ruler is 300 <br> millimetres. <br> house was exactly one kilometre. |  |
| Irregular | The distance from the scool to Arun's |  |

Mathematics
Mastery

| Numeral | A numeral is a symbol (or group of symbols) used to represent a number. | Whole numbers can all be represented as numerals consisting of the digits 0 to 9. |
| :---: | :---: | :---: |
| Obtuse angle | An angle that is greater than a right angle but less than 180 degrees. | It is greater than my right angle checker so this angle must be obtuse. |
| Parallel | Line segments that can be described as parallel must be on the same plane and will never meet, regardless of how far either or both line segments are extended. | The opposite sides of a square are parallel. |
| Perimeter | The perimeter of a 2-D shape is the total distance around its exterior. | I know that one side of this square is 2 cm so it must have a perimeter of 8 cm . |
| Perpendicular | A pair of line segments (or surfaces) can be described as perpendicular if they intersect at (or form) a right angle. | The adjacent sides of a rectangle are perpendicular. |
| Place holder | A place holder is a zero used in any place value column (that contains a value of zero) to clarify the relative positions of the digits in other places. | I need to use a place holder in the ones column to make it clear that my number is 320 and not 32 . |
| Prism | A prism is a 3-D solid with two identical, parallel bases and otherwise rectangular faces. | A triangular prism has five faces, consisting of three rectangles and two triangles which are parallel. |
| Product | The result you get when you multiply two numbers. | 24 is the product of 3 and 8 . |
| Regular | Regular 2-D shapes (regular polygons) have angles that are all equal and side lengths that are all equal. <br> Regular 3-D shapes (the Platonic Solids) are those that have congruent (exactly the same) faces of a single regular polygon. | A square is a regular 2-D shape because all four angles are right angles and all four sides are the same length. A cube is a regular 3-D shape with six identical square faces. |
| Roman numeral | Roman numerals are a system of symbols used to represent numbers that were developed and used by the Romans. They do not use a place value system. | The number twelve on this clock is represented by the Roman numerals XII, which is $10+1+1$. |
| Round | Approximate a number, normally to the nearest multiple of ten, to make it easier with which to calculate. | I would round the number 17 to 20 because it is three away from 20 but seven away from 10 . |
| Square-based pyramid | A pyramid is a 3-D shape with a 2-D shape (which gives the pyramid its name) as a base and triangular faces that taper to a point called a vertex or apex. | This square-based pyramid has five faces; one square face and four triangular faces. |
| Triangle-based pyramid |  | This triangle-based pyramid has four triangular faces. |


| Year 4 | Definition | Example |
| :---: | :---: | :---: |
| Area | The space a surface takes up inside its perimeter. Area is always measured in square units. | The area is 8 square units. |
| Associative law | No matter how the parts in an addition or multiplication equation are grouped, the answer will be the same. | $\begin{aligned} & (6+3)+2=11 \\ & 6+(3+2)=11 \end{aligned}$ <br> Addition and multiplication are associative. Subtraction and division are not. |
| Convert | To change from one unit of measurement to another. | 2 km can be converted to metres - it is equal to 2000 m . |
| Coordinate | The position of a point, usually described using pairs of numbers. Sometimes called Cartesian coordinates, after the mathematician Rene Descartes. | The coordinate $(3,4)$ describes a point that is 3 on the $x$ axis and 4 on the $y$ axis. |
| Decimal fraction | A fraction expressed in its decimal form. | Half written as a decimal fraction is 0.5 . |
| Distributive law | The process whereby adding some numbers and then multiplying the sum gives the same answer as multiplying the numbers separately and then adding the products. | $\begin{aligned} & 3 \times(2+4)=(3 \times 2)+(3 \times 4) \\ & 3 \times 12=(3 \times 10)+(3 \times 2) \end{aligned}$ |
| Dividend | The amount that you want to divide. | In '12 - 3 = 4', 12 is the dividend. |
| Divisor | The number you divide by. | In '12 $-3=4$ ', 3 is the divisor. |
| Equilateral | Having all sides the same length. | An equilateral triangle has three equal sides. |
| Equivalent | Equivalent means having the same value. Equivalent fractions have the same value. | $\frac{2}{4}=\frac{1}{2}$ |
| Expression | One or a group of numbers, symbols or operators. An expression does not use equality or inequality signs. Using an equality or inequality sign will give an equation. | $\begin{aligned} & 2 \times 3 \\ & 4^{2} \end{aligned}$ |
| Grid | A series of evenly divided and equally spaced shapes, usually squares. |  |
| Improper fraction | A fraction where the numerator is bigger than the denominator. These fractions are therefore greater than one whole. | $\frac{12}{11}$ |
| Integer | A whole number that can be positive or negative. | 6 is an integer, 0.6 is not. |
| Interval | An interval on a graph's axis lies between two values. | If one point on an axis is 50 and the next 60 , the interval is 10 . |

Mathematics
Mastery

| Isosceles | Having two sides of equal <br> length. Isosceles triangles have <br> two equal sides; isosceles <br> trapezia have wo equal, non- <br> parallel sides. |  |
| :--- | :--- | :--- |
|  | A 2-D shape with two pairs of <br> equal length adjacent sides. The <br> diagonals intersect at right <br> angles. |  |
| Kite | A graph that uses lines to <br> connect the points on a data <br> chart. <br> Used to present continuous <br> data, such as change over time. |  |
| Line graph |  |  |


| Rhombus | An equilateral parallelogram with four equal length sides. |  |
| :---: | :---: | :---: |
| Scalene | A scalene triangle has three unequal sides and three unequal angles. | $\Delta$ |
| Short division | A formal written layout where the quotient is calculated showing only one written step. | $5 \longdiv { 7 7 }$ |
| Short multiplication | A formal written layout where the multiplier is usually 9 or less. | $\begin{array}{r} 782 \\ \times \quad 9 \\ \hline 7038 \end{array}$ |
| Simplify | To write a number or equation in its simplest form. | I can simplify $\frac{8}{10}$ to $\frac{4}{5}$. |
| Square centimetre | A unit of measure for area equal to a square with the dimensions 1 cm by 1 cm . | Sometimes referred to as centimetre squared, abbreviated to $\mathrm{cm}^{2}$. |
| Trapezium | A quadrilateral with exactly one pair of parallel sides. | ] |


| Year 5 | Definition | Angles that meet at a point that <br> sum to $360^{\circ}$. |
| :--- | :--- | :--- |
| Angle at a point | Angles formed on a straight line <br> that sum to $180^{\circ}$. | A measure of central tendency. <br> The mean average of a set of <br> data is the sum of the quantities <br> divided by the number of <br> quantities. | | The mean average of the set $4,5,5,6$ is |
| :--- |
| 5 because $(4+5+5+6) \div 4=5$. |
| Average (mean) on a line |

Mathematics

Mathematics
Mastery

|  | which measures $1 \mathrm{~cm} \times 1 \mathrm{~cm} \times$ <br> 1 cm. | A unit used to measure volume. <br> The space taken up by a cube <br> with edges of length 1 metre. |
| :--- | :--- | :--- |
| Cubic metre | A polygon with ten sides and ten <br> angles. <br> metres. |  |
| Decagon | The unit of measure for angles. |  |
| one vertex to another. |  |  |

Mathematics Mastery

Mathematics
Mastery

| Prime number | A whole number with only two factors, one and the number itself. | $2,3,5,7,11,13,17$ and 19 are the prime numbers less than 20. |
| :---: | :---: | :---: |
| Remainder | The amount remaining after division when a whole number answer is needed. | 21 divided by four is equal to five with a remainder of 1. |
| Reflection | A mirror image that is equidistant from a mirror line. | The shape has been reflected in the dotted mirror line. |
| Reflex angle | An angle that is greater than $180^{\circ}$. |  |
| Scale (not to scale) | The ratio of lengths, in a drawing, are in proportion to the measurements of the real object. <br> The lengths are not in proportion when not to scale. | The diagram was not drawn to scale. That means I can't use a ruler to measure the sides, because they are not in proportion to the real object. |
| Square metre | A unit of measure for area. The surface covered by a square with sides of length one metre. | The area of the floor in a room might be measured in square metres. |
| Square number | The product of two equal factors. | 9 is a square number because $9=3 \times 3$ $=3^{2}$. |
| Tetrahedron | A 3-D shape with four triangular faces. |  |
| Transformation | A collective term for the ways that shapes can be changed, resulting in congruent or similar shapes, i.e. translation, reflection, rotation or enlargement. | Translations and reflections are types of transformations. |
| Translation | When a shape moves so that it is in a different position but retains the same size, area, angles and side length and so is congruent. | Triangle C has been translated three right and two down resulting in triangle D . |

Mathematics
Mastery

Mathematics
Mastery

| Year 6 | Definition | Ex |
| :---: | :---: | :---: |
| Arc | A portion of the circumference of a circle |  |
| Brackets | The symbols () used to separate parts of a multi-step calculation. | $(10-2) \times 3=21$ |
| Centre | In a circle, the centre refers to one point that is equidistant to all points around the circumference of the circle. | To draw a circle, I place the point of my pair of compasses at the centre. |
| Circumference | The perimeter/boundary of a circle. |  |
| Compasses | A tool for creating curved lines, arcs and circles. | I can use a pair of compasses to draw a circle with a radius of 4 cm . |
| Common fraction | A fraction written with a numerator and denominator separated by a vinculum. | One quarter can be written as a common fraction, $\frac{1}{4}$. |
| Degree of accuracy | A description of how accurately a value is communicated. | The degree of accuracy needed for the answer is one decimal place. |
| Diameter | A line from one point of the circumference of a circle to another on the opposite side, which must pass through the centre of the circle. | The circumference of a circle is the diameter multiplied by pi. |
| Equivalent expression | An expression, which can be algebraic, which is equal in value to another expression. | Find an equivalent expression to 17 + 10. $18+9$ is an equivalent expression to $17+10$. |
| Factorise | To identify factors of a given number. To express a number as factors. | I can factorise 12 by looking at its factor pairs. $1 \times 12=12,2 \times 6=12,3 \times 4=12$. So the factors of 12 are $1,2,3,4,6$ and 12. |
| Footfeet | An imperial unit of measure of length. | 1 am approximately five feet tall. |
| Formula | An algebraic expression of a rule. | The area of a rectangle can be found by multiplying the width and height. $a=w \times h$ |
| Gallon | An imperial unit of measure of volume/capacity. | A gallon is approximately 4.5 litres |
| Imperial unit | A unit of measure once officially used in the UK but is now used less often, except in the context of length. Includes miles, pounds and pints. | Miles are an imperial unit to measure length. |
| Inch | An imperial unit of measure. | An inch is approximately 2.2 cm . |
| Intersect | The point at which two (or more) lines meet is where they intersect. | The x and y axes intersect at ( 0,0 ) |

Mathematics
Mastery

| Metric unit | A standard unit of measure used in the UK and Europe. Includes centimetres, litres and kilograms. | Litres are a metric unit used to measure volume. |
| :---: | :---: | :---: |
| Mile | An imperial unit of measure of length. | Five miles is equivalent to eight kilometres. |
| Net | A group of 2-D shapes which, when folded and connected, forms a 3-D polyhedron. | The net of a cube is comprised of six connected squares. |
| Order of operations | The internationally agreed order to complete operations in a multi-step equation with multiple operations. | $(3+4) \times 2=\square$ <br> The order of operations dictates that the operation within the brackets is completed first. |
| Origin | The point at which axes in a coordinates grid cross; the point $(0,0)$. | The origin is indicated by the blue dot. |
| Ounce | An imperial unit of measure of mass. | The newborn baby had a mass of 6 pounds and 3 ounces. |
| Pie chart | A representation of a set of data where each segment represents one group in proportion to the whole. | Nationality of Astronauts on Board ISS January 2017 |
| Pint | An imperial unit of measure. | I found a pint of milk on my doorstep. |
| Pound (mass) | An imperial unit of measure of mass. | The new-born baby had a mass of 6 pounds and 3 ounces. |
| Proportion | A comparison between two or more parts of a whole or group. Proportion expresses a partwhole relationship. This may be represented as a fraction, a percentage or a decimal. | Two thirds of a class were boys. The proportion of the class that is girls is one third. |
| Quadrant | One of four regions into which a coordinates grid is divided. |  |

Mathematics

Mathematics
Mastery
\(\left.$$
\begin{array}{|l|l|l|}\hline \text { Radius } & \begin{array}{l}\text { A line from one point of the } \\
\text { circumference of a circle to the } \\
\text { centre of the circle. }\end{array} & \begin{array}{l}\text { A comparison between two or } \\
\text { more parts of a whole or group. } \\
\text { Ratio expresses a part-part } \\
\text { relationship. This is usually } \\
\text { represented in the form a:b. }\end{array}\end{array}
$$ \begin{array}{l}For every 4 tulips there are 7 daffodils. <br>

The ratio of tulips to daffodils is 4:7.\end{array}\right]\)| Ratio |
| :--- |
| have the same internal angles |
| and where the side lengths are |
| in the same ratio or proportion. |
| Enlarging a shape by a scale |
| factor (for example by doubling |
| all side lengths) creates a |
| similar shape. |$\quad$| All squares are similar to one another. |
| :--- |
| 1 mm. |

